

# Diesel Fuel Effects on Emissions: Analysis Approach

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Robert L. Mason  
Janet P. Buckingham  
Southwest Research Institute



# Overview

- Introduction
- Initial Modeling Approach
- Mixed Model Methodology
- Unified Model Approach
- Model Performance



# Overall Approach

- Construct database from existing reports and studies
  - 1777 observations on 73 engines, 300 fuels, and 16 engine tech groups
- Model diesel emissions as a function of both engine and fuel properties



# Initial Considerations

- Pre-standardize fuel properties
  - Facilitated coefficient comparisons
  - Reduced potential correlations between linear and squared fuel terms
- Transform emissions
  - Chose natural log transformation
  - Reduced variation & improved fit



# Repeat Measurements

- Some studies had multiple repeat tests
- Some had single observations and no repeats
- Some had only averages of repeat tests
  - When the number of repeats in the average was unknown, the data for the average was repeated two times



# Use of Repeats

- Initially considered limiting the number of repeats in the database
  - Constructed a file with no more than 4 repeats per engine-fuel combination
  - Randomly selected the 4 repeats
- Did this so as not to overweight data in the models



# Initial Modeling Approach

- Fit individual tech group data
- Eigenvector analysis
  - Biased estimation procedure
  - Advantageous with strong collinearities
- Stepwise mixed model analysis
  - Candidate terms included 9 linear and 3 squared fuel properties



# Mixed Model Methodology

- Contains both fixed and random effects
  - Thus labeled mixed model procedure
- Fuel properties are fixed effects
  - Controlled selection process for property values
- Engines are considered random effects
  - Engines are a sample from a population of possible engines





# Form of Mixed Model

$$Y = X\beta + Zu + e$$

where

$Y$  = emission

$X\beta$  = fixed fuel effects

$Zu$  = random engine effects

$e$  = random error terms

Assume  $u$  and  $e$  are normal with mean=0



# Applicability of Mixed Model

- Provides predictor of aggregate emissions from overall population of engines
- Adds estimation of engine variance as well as error variance to model
- Accommodates unequal variances
- Allows nesting of fuel effects within each engine



# Initial Results

- Eigenvector analysis deleted no fuel terms
  - Partitioning formula was not accurate
- Mixed model results for largest tech groups were somewhat similar
- Limited data for several tech groups
  - Some only contained a single engine
  - Had to choose terms to include in others



# Unified Model Approach

- Two-step procedure was followed
- In step 1, stepwise regression was applied
- In step 2, a mixed model with a backwards-elimination was applied
- In both cases, hierarchical models were of interest



# Use of Repeats

- Two data files were constructed
- First file contained average-repeat data
  - All repeat data were averaged
  - Singleton points were left alone
- Second file contained combined data
  - All data were included without restrictions and repeats were not averaged



# Repeat Data Usage

- Average-repeat data file was used in the stepwise regression runs
  - Maintained equal weighting of the data points
- Combined-data file was used in mixed model runs
  - Unequal weighting not an issue since repeats aid in variance estimation



# Engine-Fuel Interaction Terms

- In mixed model runs, linear fuel terms were nested within each engine term
- Done to determine if each engine had different fuel effects
- These interactions helped improve estimates of engine variation
  - Could affect significance of terms



# Stepwise Regression Approach

- Fit model in a hierarchical manner after forcing engine terms in the model
- Sequentially considered fuel terms from following groups:
  - linear fuel, squared fuel
  - fuel-fuel interactions
  - techgrp-by-fuel interactions
  - techgrp-by-squared-fuel interactions





# Stepwise Regression Procedure

- Analysis greatly simplified by automated stepwise process
- Provided quick identification of significant techgrp-by-fuel interactions
- Disadvantage included fact that some terms might be deleted early and not recognized later



# Mixed Model Approach

- Built a hierarchical model using groups of candidate variables and backwards elimination within each group
- Began with terms in last stepwise model
- Engines and engine-fuel interactions were treated as random effects
- All other terms were treated as fixed effects



# Mixed Model Backwards Procedure

Step1: Added tech group categorical variables corresponding to techgrp-by-fuel interactions in model

Step 2: Removed nonsignificant techgrp-by-fuel interactions in backward process

- Retained nonsignificant linear interaction if quadratic interaction was significant



# Mixed Model Procedure

Step 3: Deleted nonsignificant tech group terms unless part of model hierarchy for techgrp-by-fuel interactions

Step 4: Deleted nonsignificant fuel-by-fuel interaction terms

Step 5: Deleted nonsignificant linear fuel terms, unless needed for model hierarchy



# Mixed Model Results

Final model contained terms with significant coefficients, as well as terms with nonsignificant coefficients that were needed to maintain good model hierarchy



# Model Performance

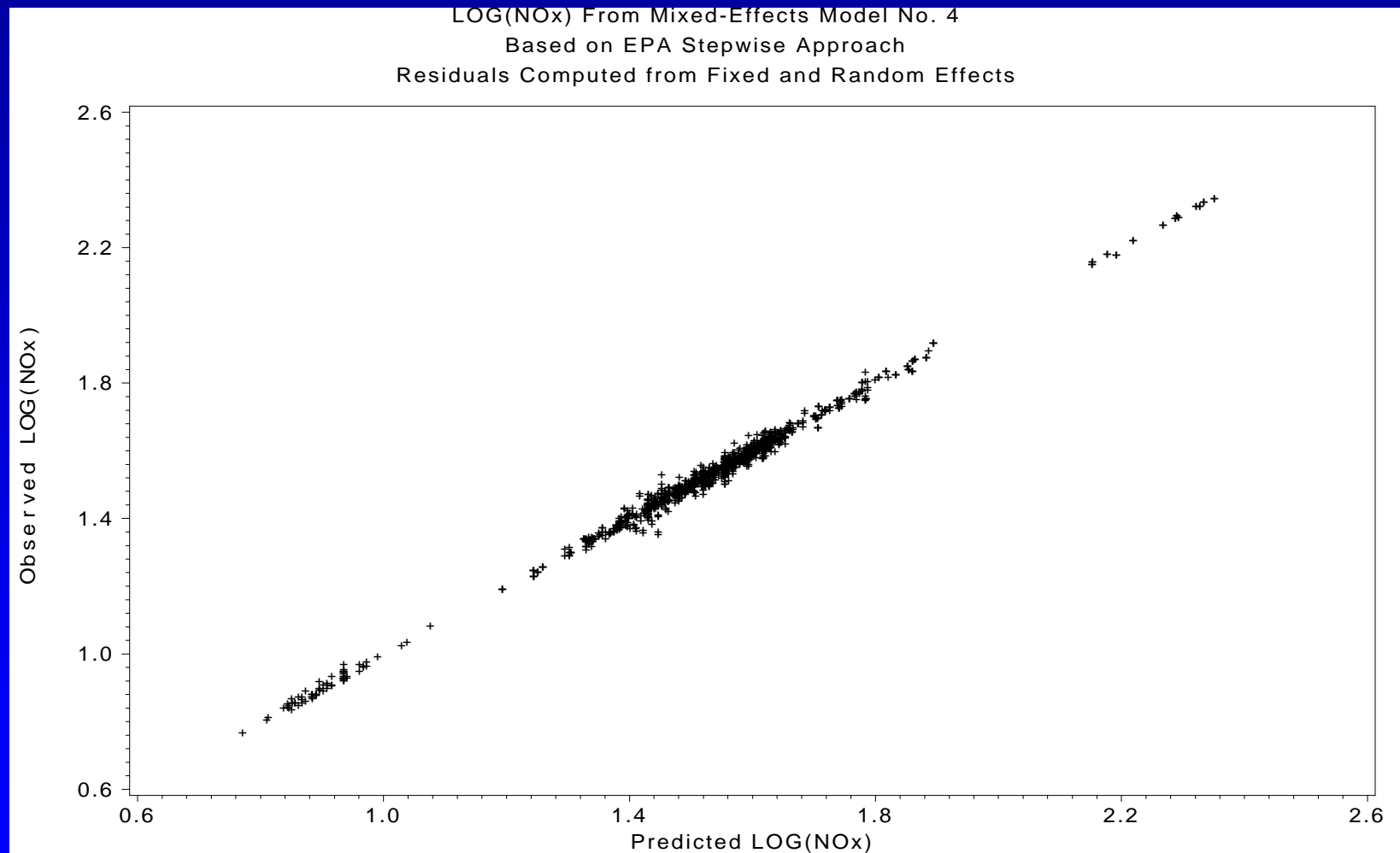
- Based on comparing Observed and Predicted % Change in Emissions relative to a national average base fuel

$$\text{Obs \% CE} = 100\%(\text{ObsFuel}/\text{ObsBase}-1)$$

$$\text{Prd \%CE} = 100\%(\text{PrdFuel}/\text{PrdBase}-1)$$



# Model Performance Results



# Model Performance Results

Cumulative % of the absolute differences  
between observed and predicted %CE  
that are between +/-10%

NOx	99%
PM	81%
HC	47%





# NOx Model Results

Variable	Stepwise Model	Mixed Model No Natural Cetane Interaction with Engines	Mixed Model
INTERCEPT	<b>1.61682</b>	<b>1.5326</b>	<b>1.5312</b>
NATURAL CETANE	<b>-0.00751</b> (p=0.0007)	-0.00309 (p=0.0751)	-0.00033 (p=0.9047)
CETANE DIFFERENCE	<b>-0.01267</b>	<b>-0.01145</b>	<b>-0.01187</b>
TOTAL AROMATICS	<b>0.02779</b>	<b>0.02654</b>	<b>0.02679</b>
SPECIFIC GRAVITY	<b>0.01553</b>	<b>0.02195</b>	<b>0.02375</b>
SULFUR	0.00230	0.000932	0.000644
T10	-0.00101	0.004796	0.003553
T50	<b>-0.00978</b>	<b>-0.01396</b>	<b>-0.01459</b>



# Summary

- Initial modeling approach led to use of combined database rather than individual tech group database
- Chosen methodology was combination of stepwise regression and mixed model
- Major advantage was the ability to predict aggregate emissions for overall population of engines represented by sample



# Summary

- Prediction equations used to predict % change in emissions relative to a baseline fuel
- Model performance based on comparing observed and predicted % change in emissions

